



NEWS FROM THE ELECTROWEAK SM FIT AND CONSTRAINTS ON SM EXTENSIONS

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for the Gfitter Group*

LoopFest XI, Pittsburgh
May 11th 2012

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INTRODUCTION TO GFITTER

REFERENCE PAPER:
EPJ C60, 543-583,2009 [ARXIV:0811.0009]
UPDATE & BSM:
ACCEPTED BY EPJ C, [ARXIV:1107.0975]
[HTTP://WWW.CERN.CH/GFITTER](http://www.cern.ch/gfitter)

1. Goal

- provide state-of-the-art model testing tool for LHC era

2. Input to Gfitter

- electroweak precision measurements from **LEP, SLD, Tevatron und LHC**
- **theoretical predictions**

3. The Gfitter Package

- C++, ROOT, xml
- Core Package: data handling, fitting and statistics tools
- full statistics analysis
 - parameter scans
 - p-values
 - toy MC analyses
 - goodness-of-the-fit tests
- physics libraries



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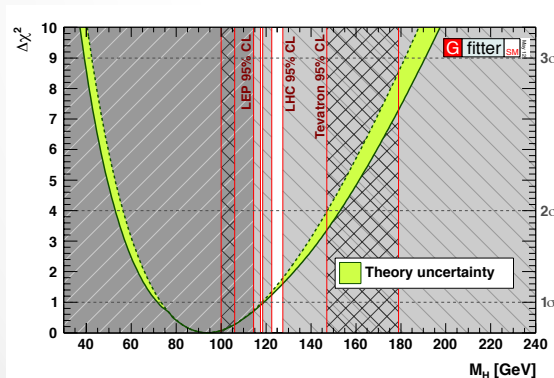
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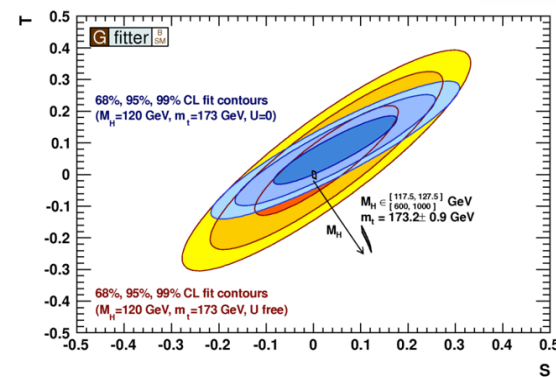
4. SM: global electroweak Fit

- constraints on M_H
- constraints on M_W, m_t
- determination of $\alpha_S, \sin^2\theta_{\text{eff}}$, pull-values of electroweak observables

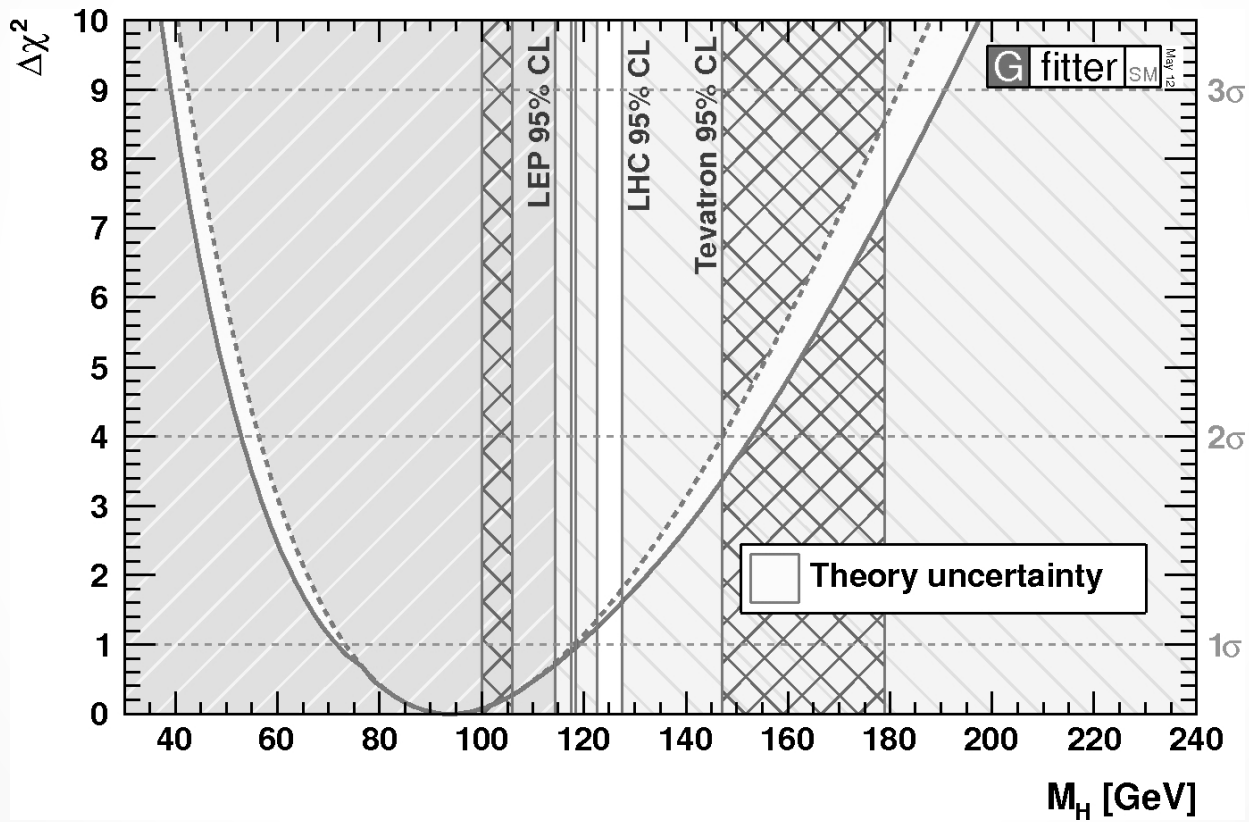


5. BSM physics models – STU Parameter

- introduce oblique parameters
- ew fit - sensitive to BSM physics through oblique corrections
- SM vs. BSM physics



THE ELECTROWEAK FIT WITH GFITTER



The Electroweak Fit: Experimental Input I

- Z-pole observables including their correlations: LEP/SLD experiments

[ADLO+SLD, Phys. Rept. 427, 257 (2006)]

- new W mass measurements from D0 and CDF combined with LEP result:

$$M_W = 80.385 \pm 0.015 \text{ GeV}$$

[ADLO, hep-ex/0612034][D0, arXiv:1203.0293]

[CDF, arXiv:1203.0275][LEPEWWG]

- Γ_W : LEP/Tevatron

[ADLO, hep-ex/0612034][CDF& D0, arXiv:0908.1374]

- m_c, m_b : world averages

[PDG, J.Phys.G G37 (2010)]

- m_t : Tevatron using 5.8 fb^{-1}

[D0& CDF, arXiv:1107.5255]

- $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$: including α_s dependency

[Davier et al. EPJ C71 (2011)]

- Dörthe Kennedy – EW Fit with Gfitter

Parameter	Input value	Free in fit
M_Z [GeV]	91.1875 ± 0.0021	yes
Γ_Z [GeV]	2.4952 ± 0.0023	–
σ_{had}^0 [nb]	41.540 ± 0.037	–
R_ℓ^0	20.767 ± 0.025	–
$A_{\text{FB}}^{0,\ell}$	0.0171 ± 0.0010	–
$A_\ell^{(*)}$	0.1499 ± 0.0018	–
A_c	0.670 ± 0.027	–
A_b	0.923 ± 0.020	–
$A_{\text{FB}}^{0,c}$	0.0707 ± 0.0035	–
$A_{\text{FB}}^{0,b}$	0.0992 ± 0.0016	–
R_c^0	0.1721 ± 0.0030	–
R_b^0	0.21629 ± 0.00066	–
$\sin^2\theta_{\text{eff}}^\ell(Q_{\text{FB}})$	0.2324 ± 0.0012	–
M_H [GeV] ^(o)	95% CL limits	yes
M_W [GeV]	80.385 ± 0.015	–
Γ_W [GeV]	2.085 ± 0.042	–
\bar{m}_c [GeV]	$1.27^{+0.07}_{-0.11}$	yes
\bar{m}_b [GeV]	$4.20^{+0.17}_{-0.07}$	yes
m_t [GeV]	173.2 ± 0.9	yes
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ ^(†Δ)	2757 ± 10	yes
$\alpha_s(M_Z^2)$	–	yes
$\delta_{\text{th}} M_W$ [MeV]	$[-4, 4]_{\text{theo}}$	yes
$\delta_{\text{th}} \sin^2\theta_{\text{eff}}^\ell$ ^(†)	$[-4.7, 4.7]_{\text{theo}}$	5 yes

The Electroweak Fit: Experimental Input II

- direct **Higgs mass** exclusions (at 95% CL):
 - **LEP: $M_H > 114$ GeV**
[ADLO: Phys. Lett. B565, 61 (2003)]
 - **Tevatron: 100-119 GeV and 141-184 GeV**
[TEVNPH: arXiv:1203.3782]
 - **ATLAS: 110-117.5 GeV, 118.5-122.5 GeV, and 129-539 GeV**
[ATLAS-CONF-2012-019]
 - **CMS: 127.5-600 GeV**
[CMS-PAS-HIG-12-008]
 - **LHC+Tevatron: excess at 125 GeV**

Allowed Regions

- 117.5 – 118.5 GeV
- 122.5 – 127.5 GeV

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$\delta_{\text{th}}\sin^2\theta_{\text{eff}}^\ell$ ^(t)	$[-4.7, 4.7]_{\text{theo}}$	6 yes

The Electroweak Fit: Theoretical Input I

- electroweak precision observables expressed as functions of the free SM parameters:

$$M_Z, M_H, m_t, \Delta\alpha^{(5)}_{\text{had}}(M_Z^2), \alpha_s(M_Z^2), m_c, m_b$$

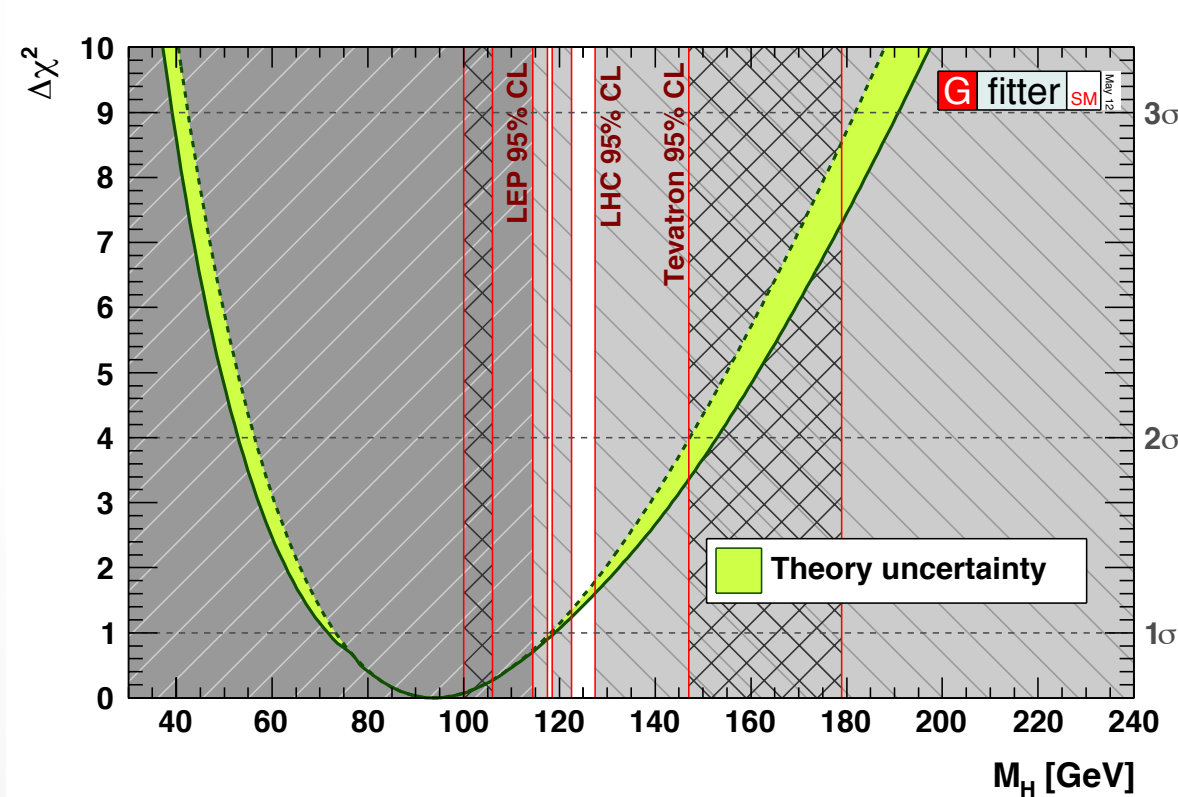
- most important predictions for constraining the Higgs mass
 - M_W and $\sin^2\theta_{\text{eff}}^f$: full two-loop + leading beyond-two-loop correction
[M. Awramik et al., Phys. Rev D69, 053006 (2004)][M. Awramik et al., JHEP 11, 048 (2006), M. Awramik et al., Nucl.Phys.B813:174-187 (2009)]
 - theoretical uncertainties (due to e.g. truncation of higher QCD orders):
 M_W ($\delta M_W = 4 \text{ MeV}$) and $\sin^2\theta_{\text{eff}}^f$ ($\delta \sin^2\theta_{\text{eff}}^f = 4.7 \cdot 10^{-5}$)
 - $\sin^2\theta_{\text{eff}}^f$ defines asymmetry parameter and forward-backward asymmetry
- width of W boson not crucial for fit due to large experimental uncertainty
[Hagiwara et al., arXiv:1104.1769)]

The Electroweak Fit: Theoretical Input II

- partial Z widths (or ratio of them)
 - important for determination of α_s
 - Z couplings implemented by parametrization
 - one-loop, partly at two-loop level for $O(\alpha\alpha_s)$
[Hagiwara et al., arXiv:1104.1769]][more information in DESY-THESIS-2011-029]
 - Correction applied for large Higgs masses ($M_H > 500$ GeV)
 - accounting for difference between ZFitter and parametrization
[Bardin et al, CPC 133,299(2001)][Arbuzov et al., CPC 174,728(2006)]
 - radiator functions describe final QCD and QED radiation
[Hagiwara et al, Z.Phys. C64, 559 (1994), Bardin et al. ,The standard model in the making (1999), Bardin et al., CPC. 133, 229 (2001)]
 - including N3LO to hadronic Z decay
[P.A. Baikov et al., Phys. Rev. Lett. 101 (2008) 012022, P.A. Baikov et al., arXiv:1201.5804 [hep-ph]]
- Include new R_b calculation
[Freitas and Huang, arxiv:1205.0299]

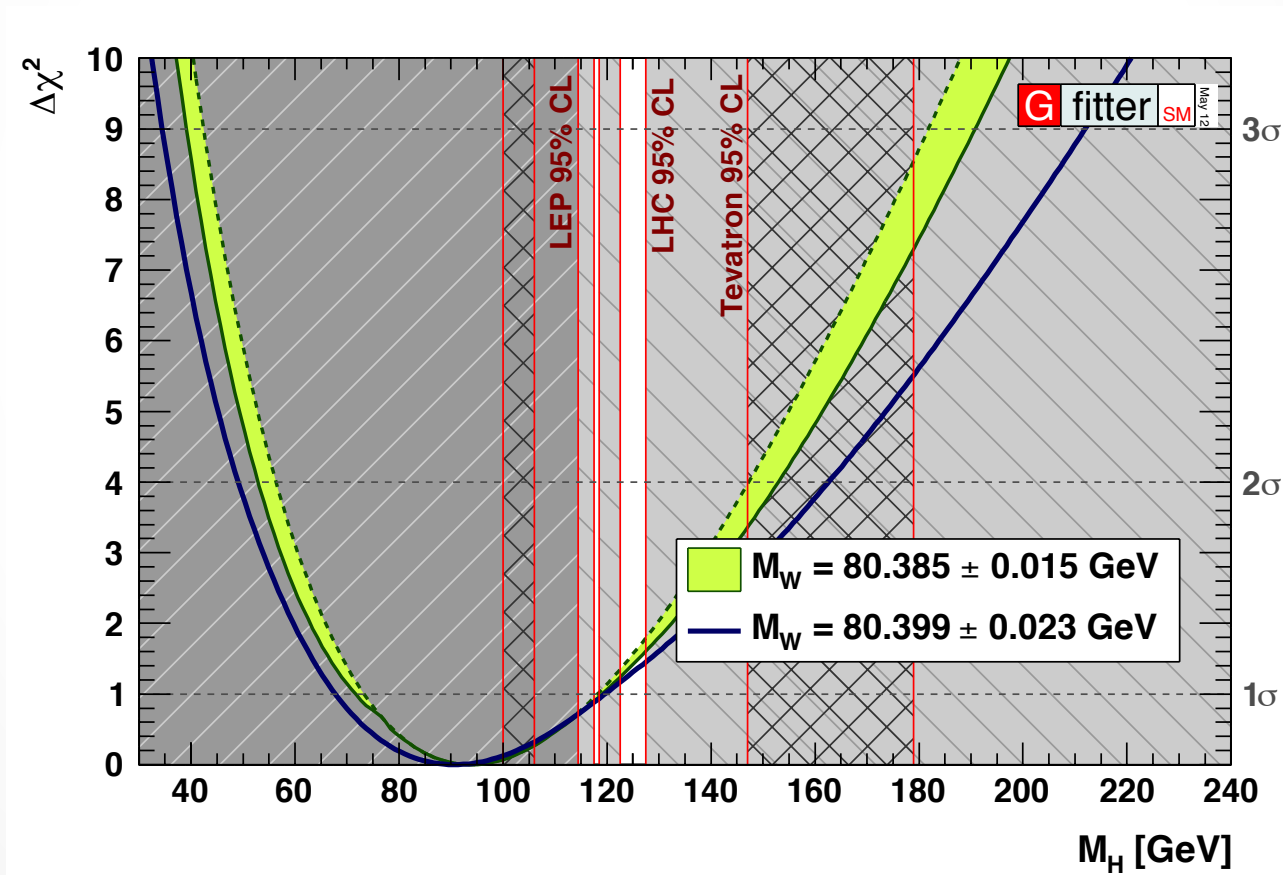
The Electroweak Fit: Constraints on Higgs mass

- M_H from fit including all data except results from direct Higgs searches at LEP, Tevatron, LHC
 - value at minimum $\pm 1\sigma$: $M_H = 94^{+25}_{-22}$ GeV
- 95% (99%) upper bound: 152 GeV (176 GeV)

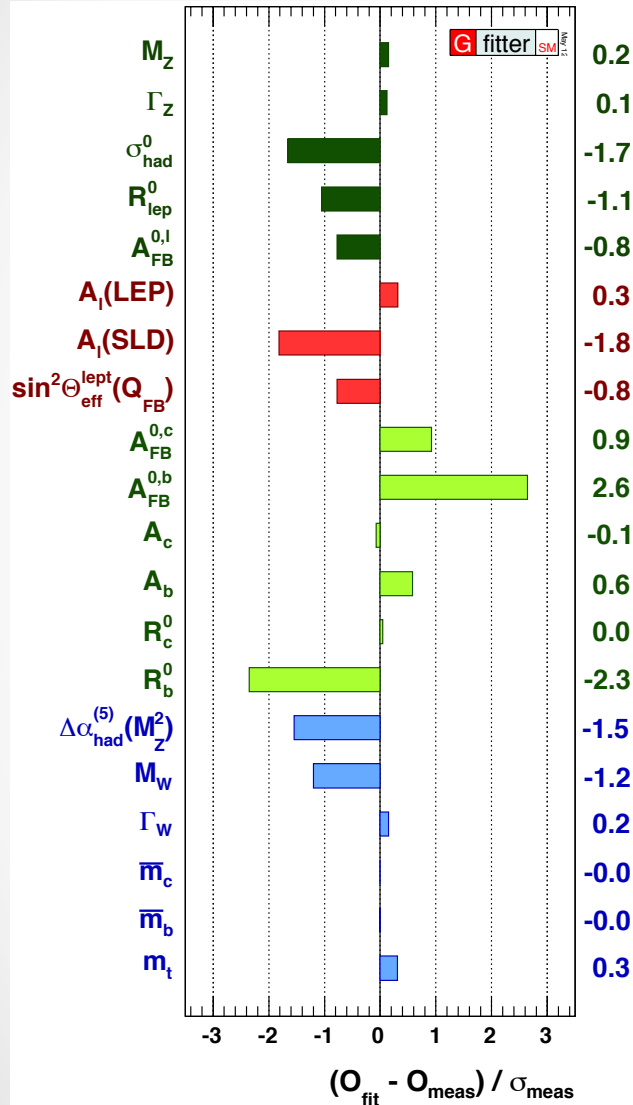


The Electroweak Fit: New M_W

- new M_W measurement improves the 95% and 99% CL limits



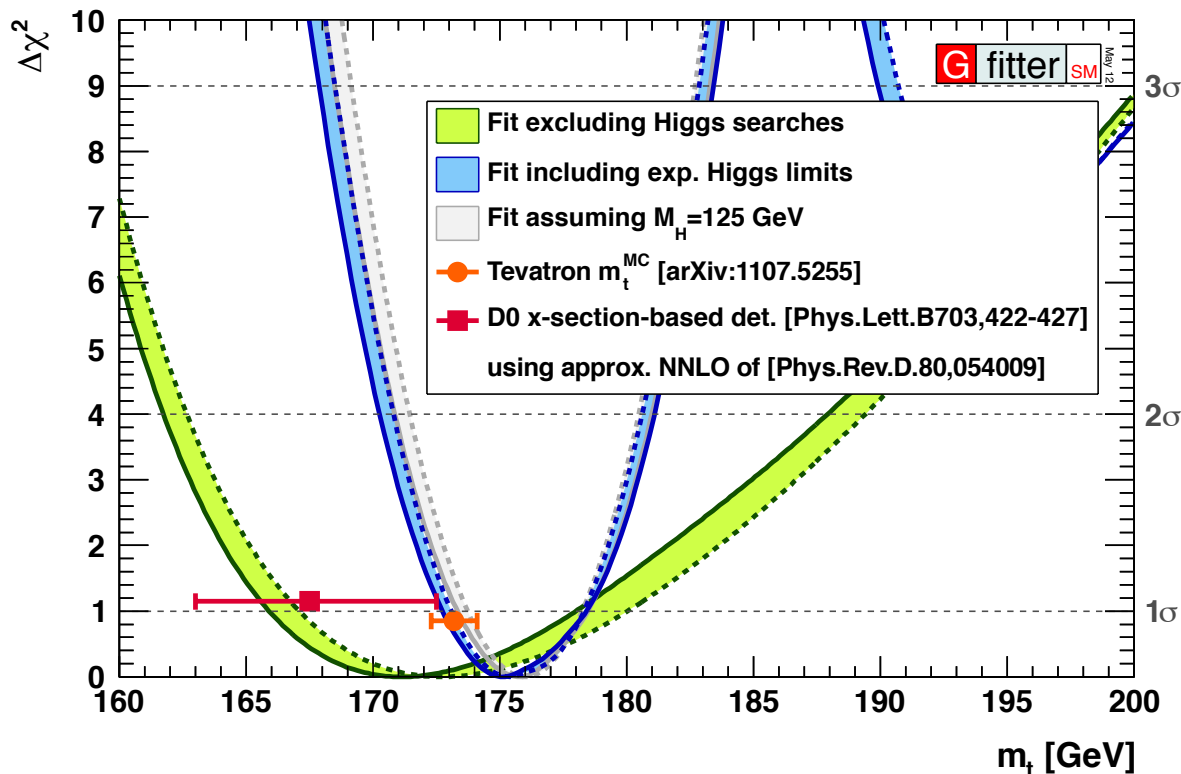
The Electroweak Fit: SM Fit Results



- goodness-of-the fit:
 - excl. (incl.) direct Higgs searches:
 - $\chi^2_{\text{min}} = 20.3$ (21.8)
 - $\text{Prob}(\chi^2_{\text{min}}, 13(14)) = 0.09$ (0.08)
 - reduced by new R_b calculation
 - values before 2011:
 - $\chi^2_{\text{min}} = 16.6$ (17.8)
 - $\text{Prob}(\chi^2_{\text{min}}, 13(14)) = 0.21$ (0.23)
- pull values (incl. direct Higgs searches)
 - increased pull-value of R_b : $-0.8 \rightarrow -2.3$
 - $A_{\text{FB}}^{0;b}$ largest contributor to χ^2_{min}
 - no individual pull exceeds 3σ
 - small contributions from M_Z , $\Delta \alpha_{\text{had}}^{(5)}(M_Z^2)$, m_c , m_b
 - input accuracies exceed fit requirements
- good agreement between data and SM

The Electroweak Fit: Determination of m_t

- direct top mass measurement is not included
 - fit excluding (including) direct Higgs searches
 - fit with fixed Higgs mass
- fit results in agreement with direct measurements



w/o direct Higgs searches

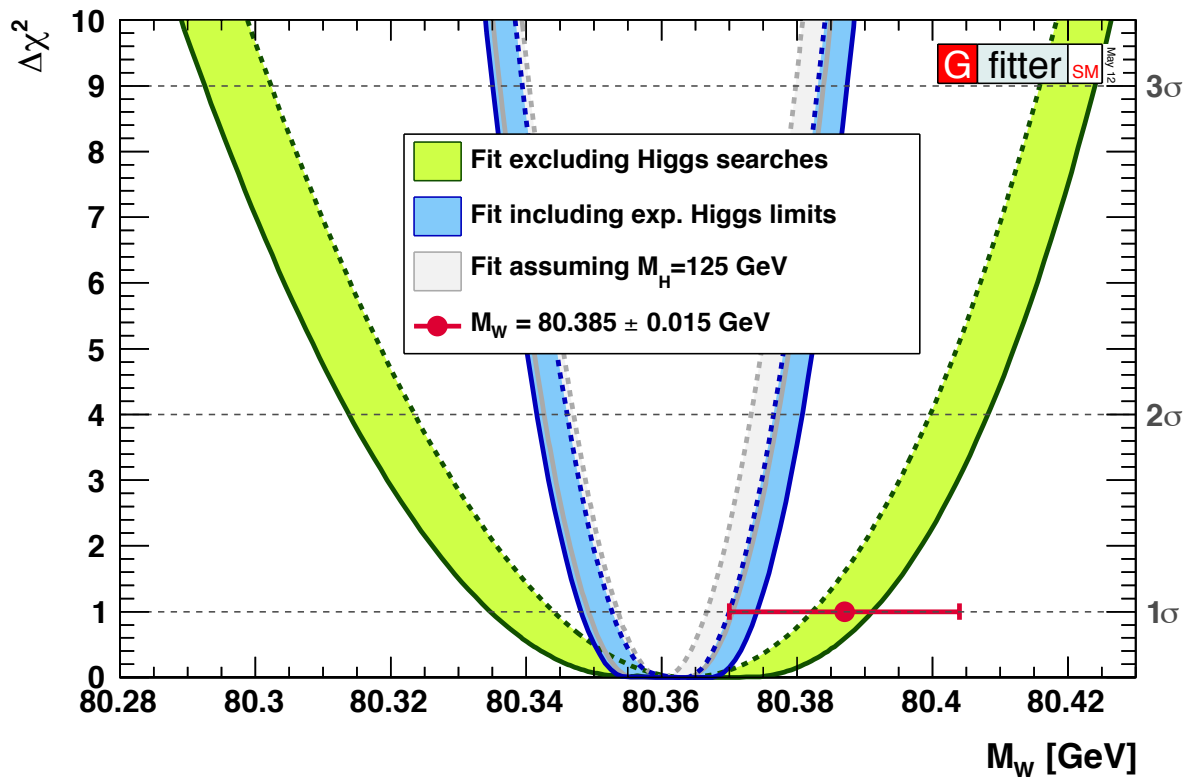
• $171.1^{+6.8}_{-5.2}$ GeV

with direct Higgs searches

• $175.1^{+3.3}_{-2.4}$ GeV

The Electroweak Fit: Determination of M_W

- direct W mass measurement is not included
 - fit excluding (including) direct Higgs searches
 - fit with fixed Higgs mass
- fit results in agreement with direct measurements
- indirect determination higher precision than world average



w/o direct Higgs searches

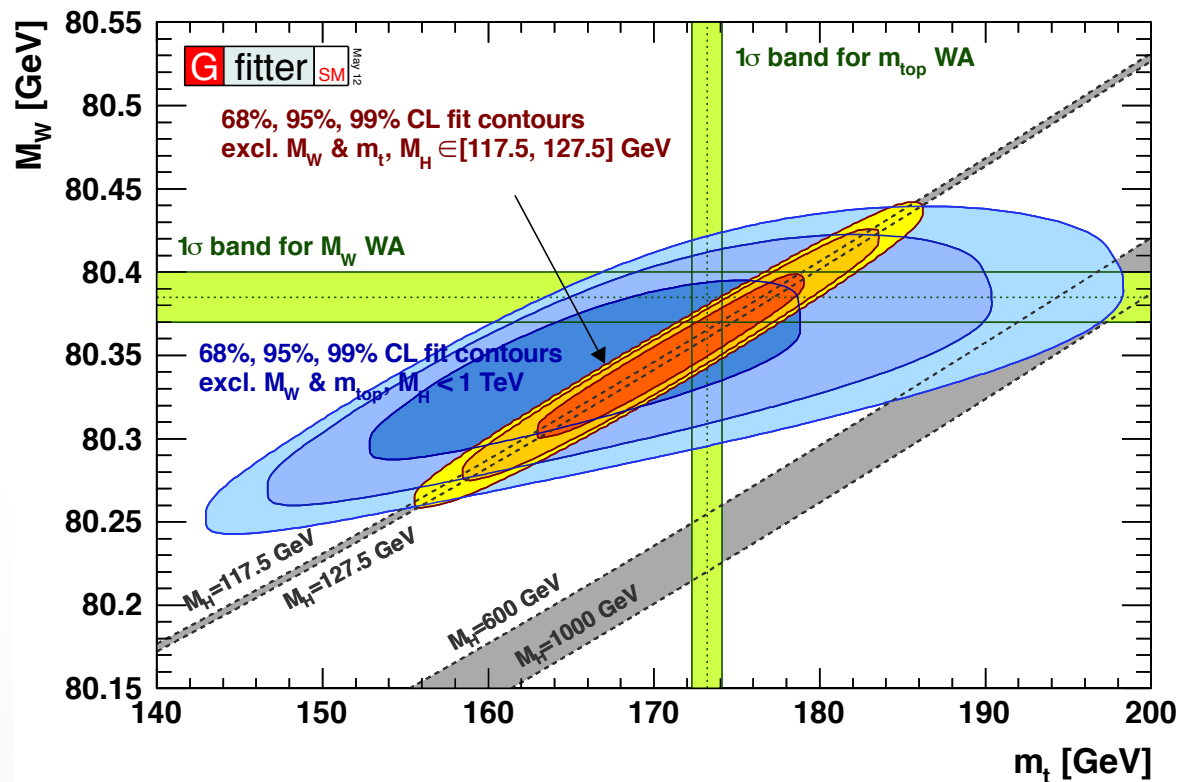
• 80.363 ± 0.028 GeV

with direct Higgs searches

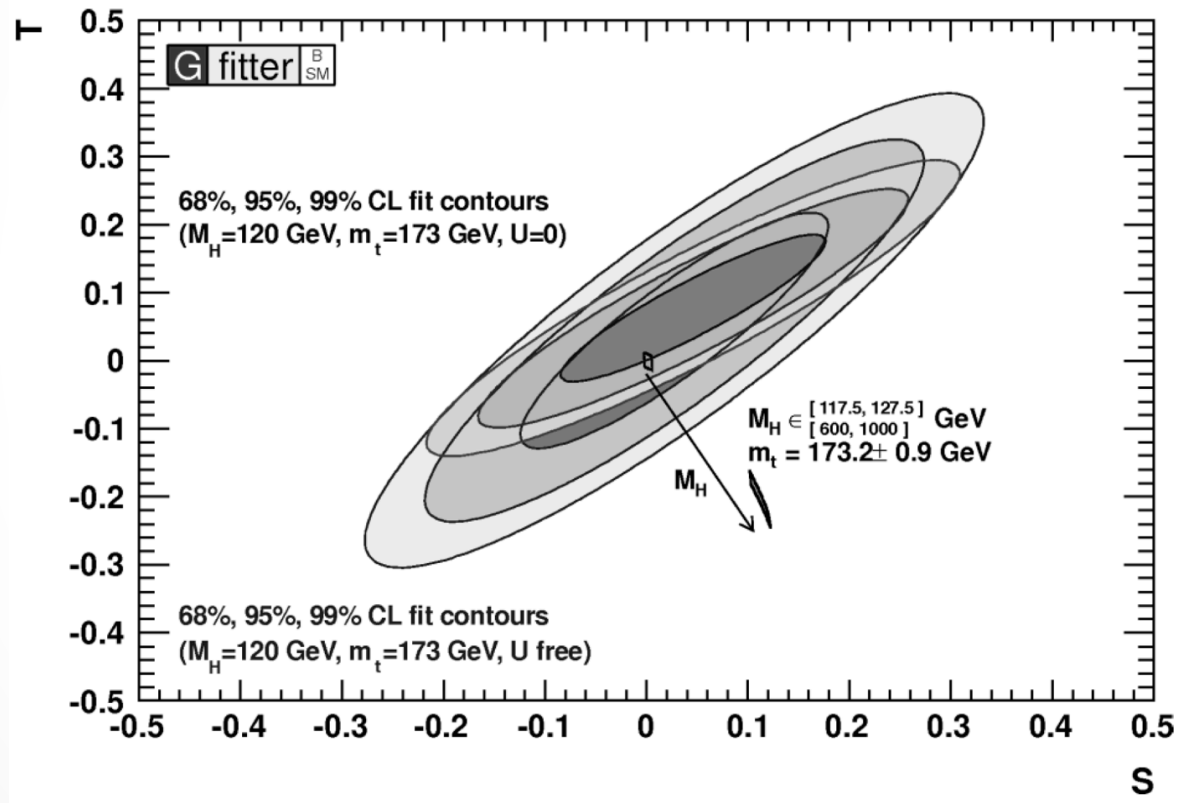
• 80.361 ± 0.013 GeV

The Electroweak Fit: Scan of m_t and M_W

- green bands: world average, agree with indirect constraints
- direct Higgs searches constrain both observables significantly
- possible to probe SM or BSM physics models



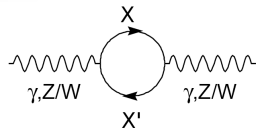
CONSTRAINTS ON NEW PHYSICS MODELS



”OBLIQUE” PARAMETERS

[Peskin and Takeuchi, Phys. Rev. D46, 1 (1991)]

1. **assumption:** high-scale BSM physics appears only through **vacuum polarisation corrections** (cf. rad. corr. from m_t , MH in SM)



2. ew fit sensitive to BSM physics through these **oblique corrections**

3. **oblique corrections** from New Physics described through **STU parametrization**

$$O = O_{SM;ref}(M_H; m_t) + c_S S + c_T T + c_U U$$

4. **STU measure deviations** from electroweak radiative correction expected in SM_{ref}

S: new physics contribution to **neutral current processes**

U: (+S) new physics contribution to **charged current processes**

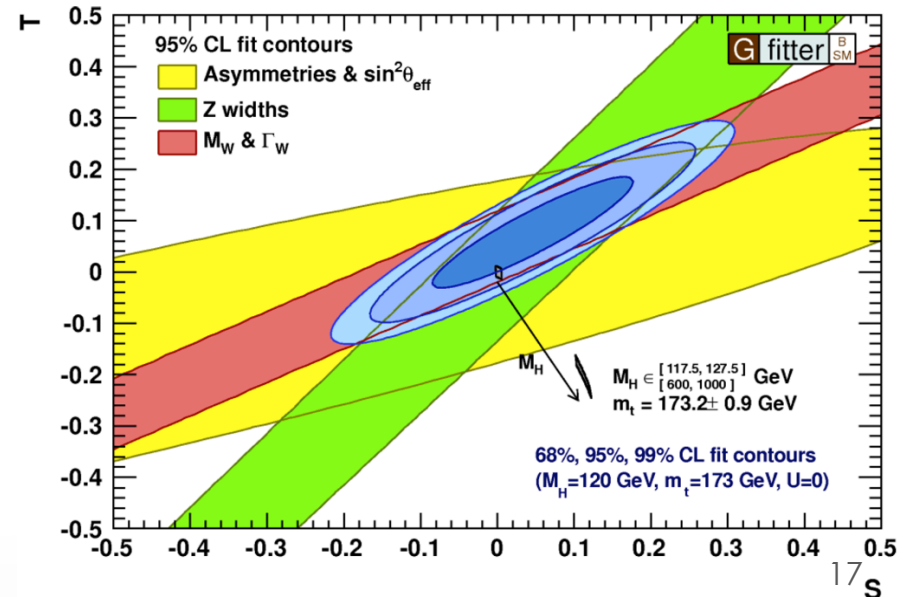
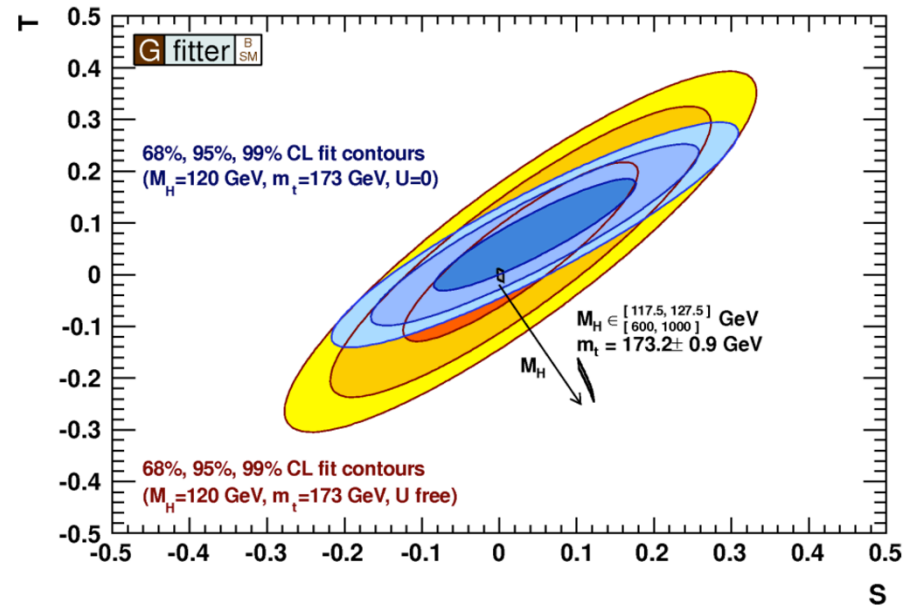
- U only sensitive to M_W and Γ_W
- usually very small in new physics models (often: $U=0$)

T: **difference** between neutral and charged current processes

- sensitive to weak isospin violation

Fit of S-T-U

- S, T, U derived from fit to electroweak observables
 - SM_{ref} : $m_t = 173 \text{ GeV}$, $M_H = 120 \text{ GeV}$
- results for STU:
 - $S = 0.04 \pm 0.10$, $T = 0.05 \pm 0.11$,
 $U = 0.08 \pm 0.11$
- gray area: SM prediction
 - for SM_{ref} : $S = T = U = 0$
 - S, T: logarithmically dependent on M_H
 - small M_H compatible with data
- BSM physics models
 - large S-T area allowed due to unconstrained model parameters
 - heavy Higgs masses due to compensation
- status of recent publication
 - update is in progress
 - new m_t , M_H partially included
 - no new M_W , R_b , N3LO to hadronic Z decay



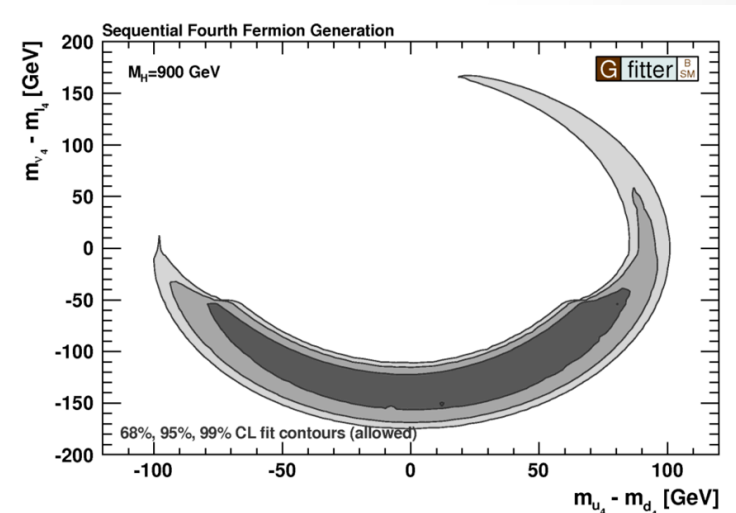
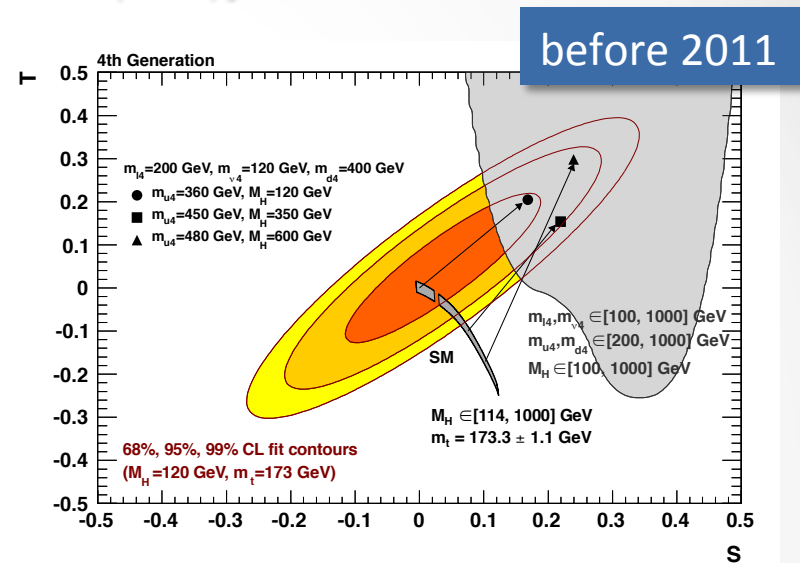
SEQUENTIAL FOURTH GENERATION

[Hubisz et al., JHEP 0601:135 (2006)]

- models with a fourth generation
 - SM: no explanation for $n=3$ generations
 - introduction of new states for leptons and quarks

$$\Psi_L = (\Psi_1, \Psi_2)_L, \Psi_{1,R}, \Psi_{2,R}$$

- free parameters:
 - masses of new quarks and leptons
 $m_{u4}, m_{d4}, m_{e4}, m_{\nu4}$
 - assuming: no mixing of extra fermions
 - model-independent
- contribution to STU from new fermions
- sensitivity to mass difference between up-type and down-type elds, rather than absolute mass scale
- results:
 - with appropriate mass differences: 4th fermion model consistent with data
 - large M_H is allowed
 - data prefer a heavier charged lepton



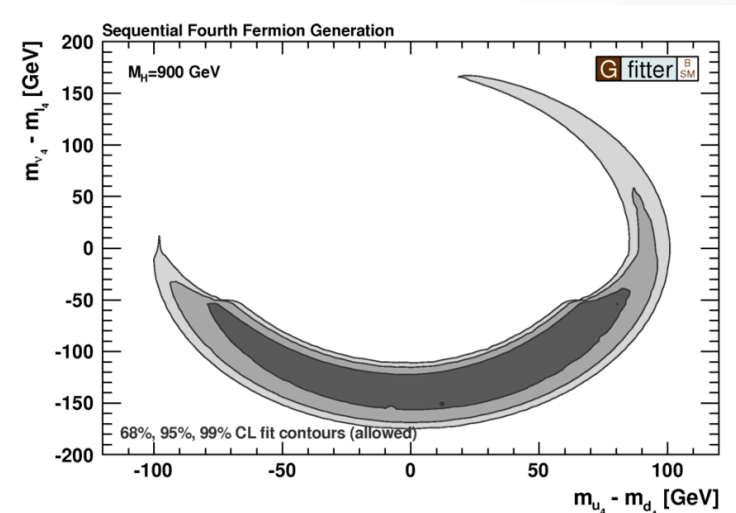
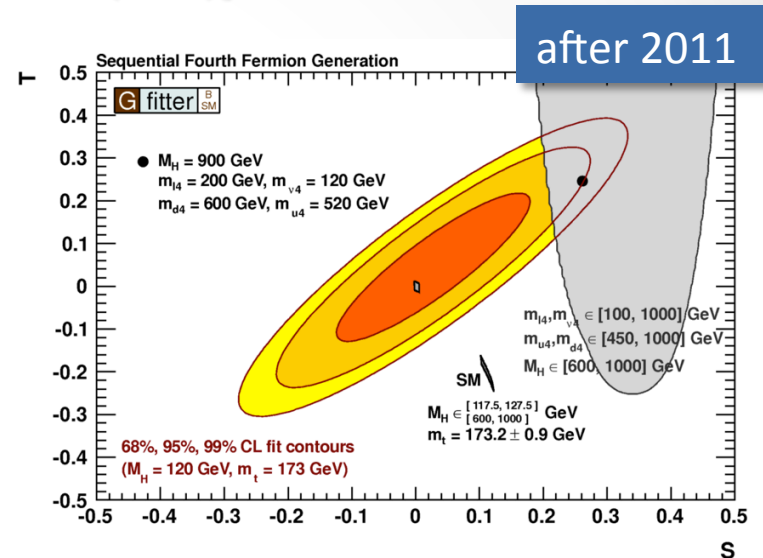
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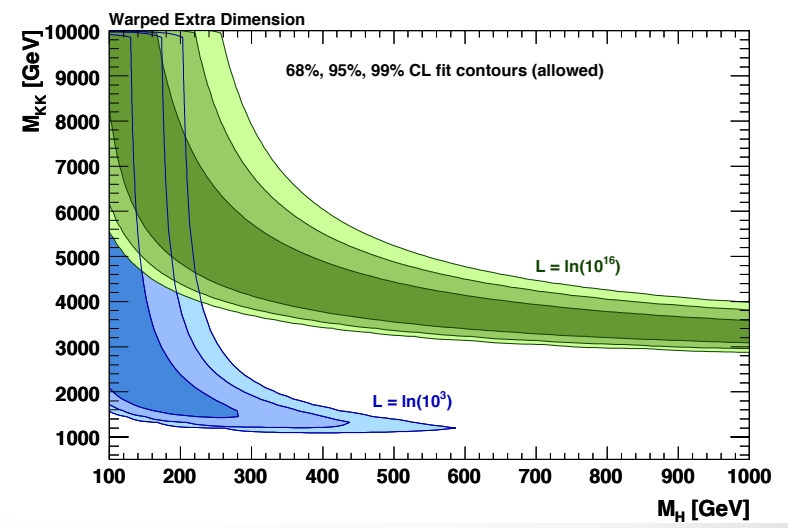
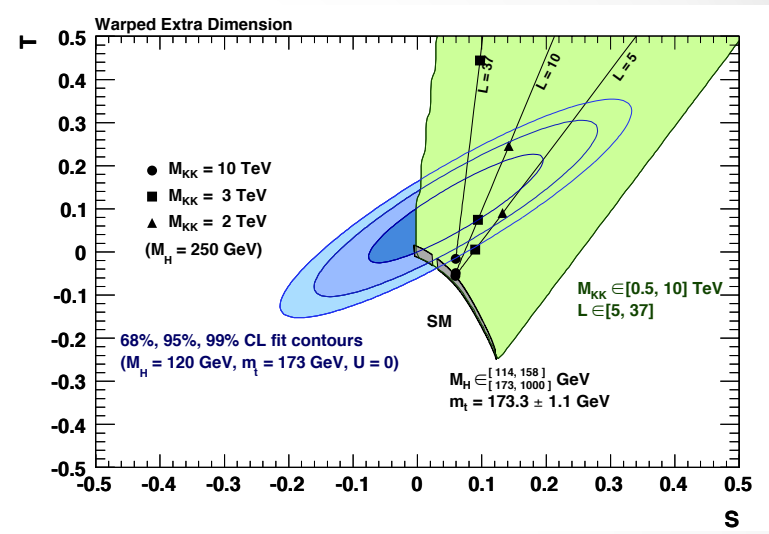
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WARPED EXTRA DIMENSION

[L.Randall, R.Sundrum, Phys. Rev. Lett. 83, 3370 (1999)] [S. Casagrande et al., JHEP10(2008)094]

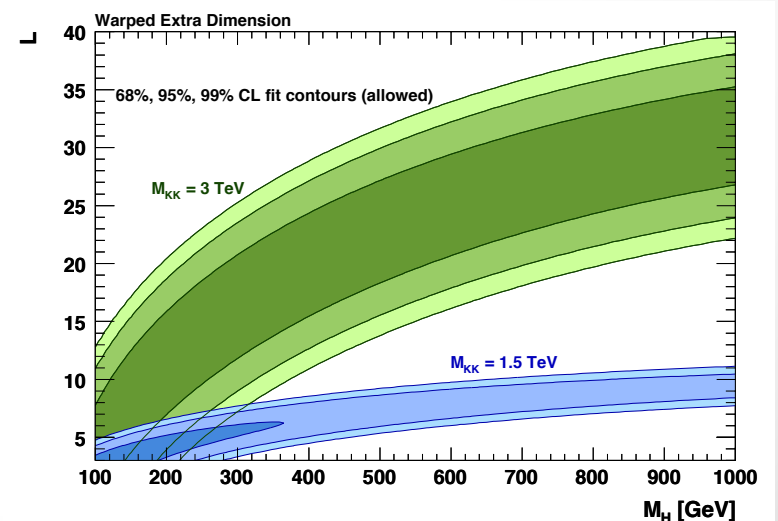
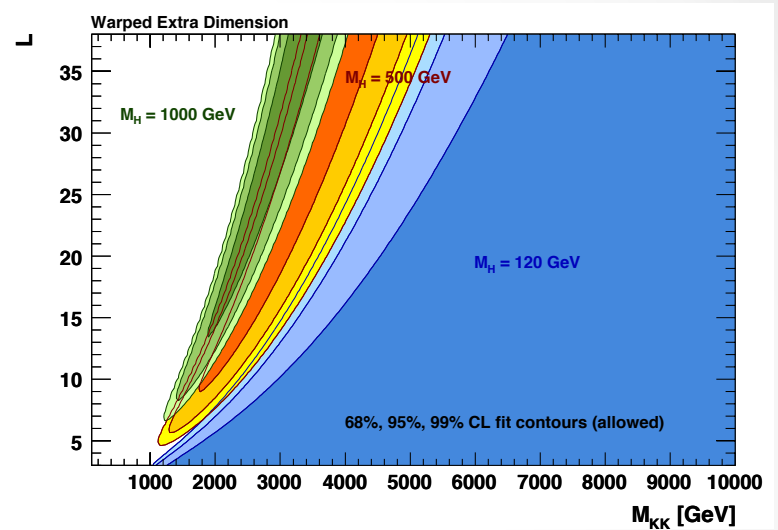
- extra dimension (ED) confined by two branes for solving hierarchy problem
- generation of weak scale on IR brane from UV brane: introduction of warp factor (exp. func. of compactification radius of ED)
- originally: ED only accessible to gravity
- here: SM fermions, gauge bosons propagate into bulk, Higgs does not
- free parameters
 - M_{KK} : KK scale (heavy KK modes)
 - L : log of warp factor
- results:
 - large L requires large M_{KK}
 - compensation if M_H is large



WARPED EXTRA DIMENSION

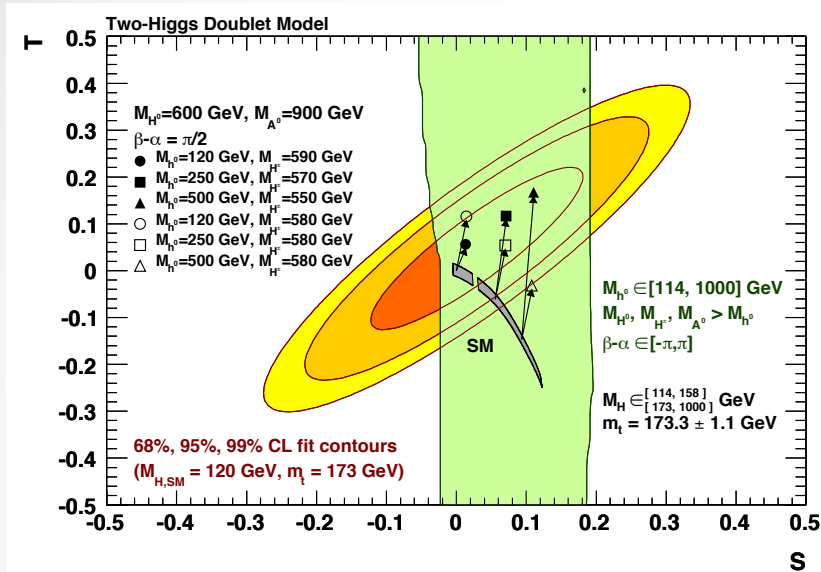
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Two-Higgs Doublet Model I

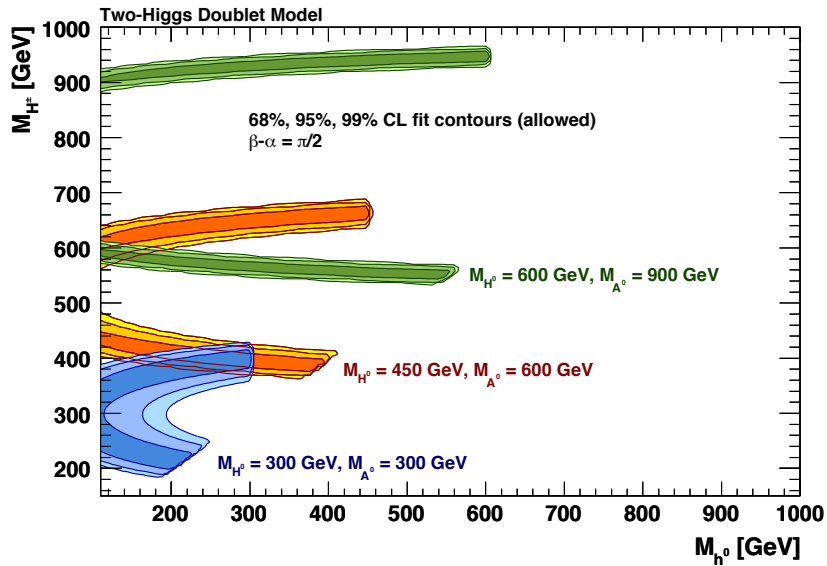
[H. E. Haber et al., Nucl. Phys. B161, 493 (1979).],[C. D. Froggatt et al., Phys. Rev. D45, 2471 (1992).]



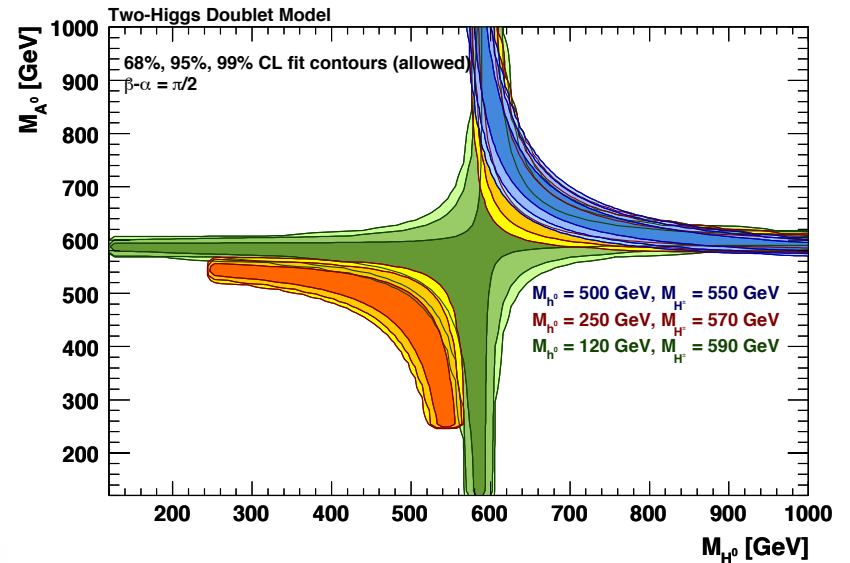
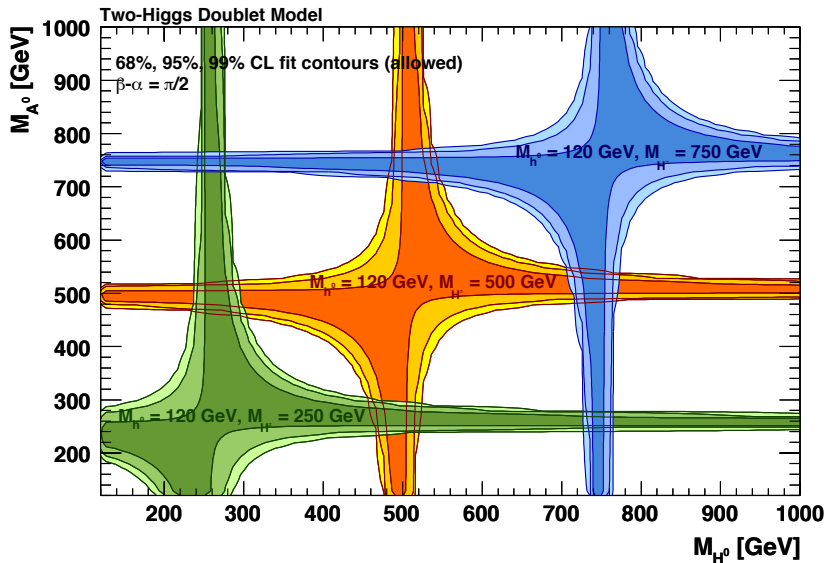
- different 2HDM types:
 - Type-I: only one doublet couples to fermion sector
 - Type-II: one doublet couples to up-type fermions, one to down-type fermions, resembles Higgs sector of MSSM
 - type distinction irrelevant for study of oblique corrections
 - defined according to Yukawa couplings, do not enter oblique corrections at one-loop order
- free parameters:
 - Higgs masses $M_{h_0}, M_{H_0}, M_{A_0}, M_H$
LEP limit: $M_H > 78.6 \text{ GeV}$
 - ratio of the vev of the two doublets, $\tan\beta = v_2/v_1$ (mixing of charged and neutral fields)
 - angle α (mixing of the neutral CP-even Higgs fields)

Two-Higgs Doublet Model II

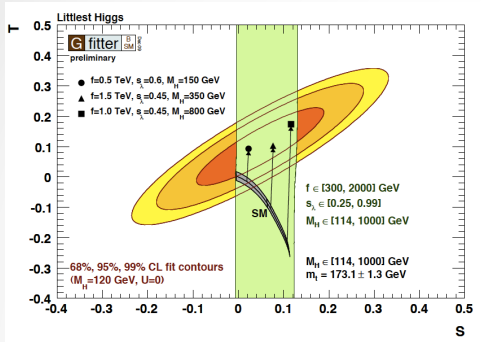
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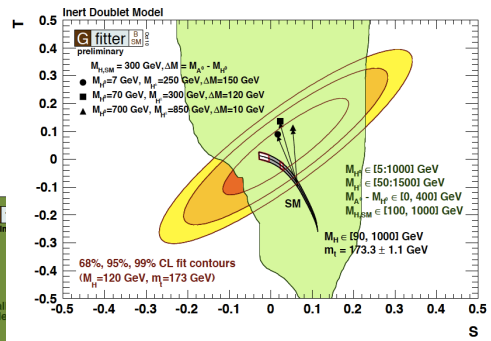
- parameter constraints only dependent of other parameters
- for light M_{h^0} :
 - similar values of the heavy Higgs masses preferred



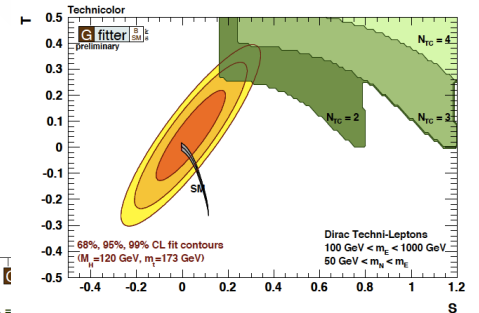
MANY MORE MODELS



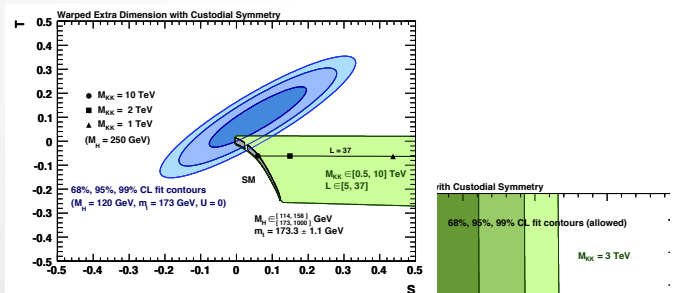
Littlest Higgs Model



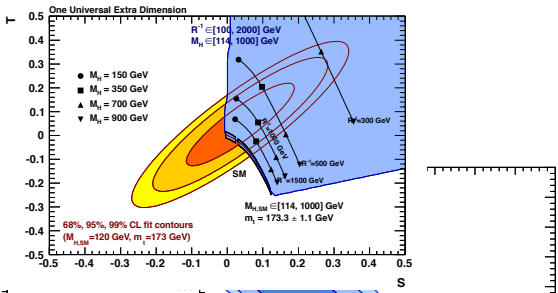
Inert Doublet Model



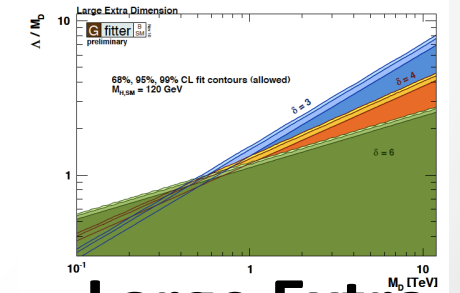
Technicolor



Warped Extra Dimension With Custodial Symmetry



One Universal Extra Dimension

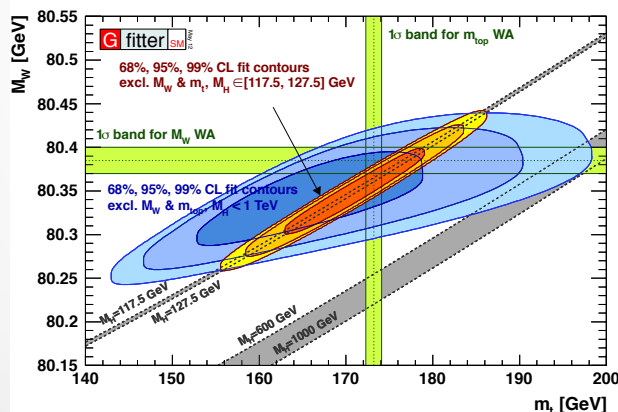


Large Extra Dimensions

CONCLUSION

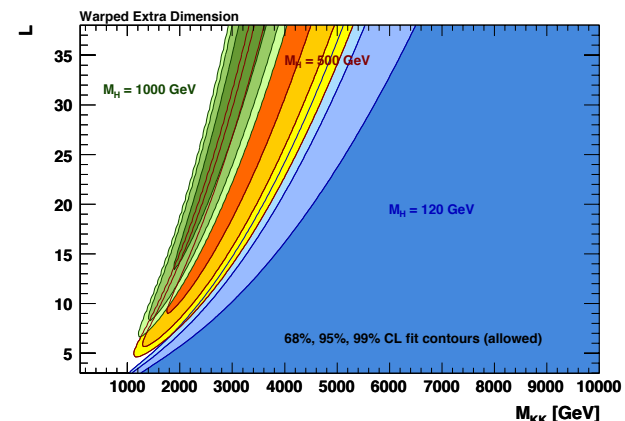
Standard Model

- global fit of the electroweak SM
- good compatibility of the SM and the electroweak precision data
- inclusion of latest direct Higgs searches
 - Higgs mass strongly constrained
 - light Higgs preferred by SM
- inclusion of the latest R_b calculations



BSM physics models

- test compatibility of various BSM models with electroweak precision data via the oblique parameters
- set constraints on BSM model parameters
- heavier Higgs boson allowed in various BSM models



THANK YOU FOR YOUR ATTENTION!



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UPDATE & BSM: ACCEPTED BY EPJ C, [ARXIV:1107.0975]

[HTTP://WWW.CERN.CH/GFITTER](http://WWW.CERN.CH/GFITTER)

BACKUP

...

STATISTICAL INTERPRETATION OF DIRECT HIGGS SEARCHES

- Statistical interpretation
 - Experiments measure test statistic
 - Transformed by experiments into 1-sided upper limit (CL_S=CL_S+B/CL_B) using pseudo experiments
 - We transform 1-sided CL_S+B into 2-sided CL_{2s}+B
 - SM is null hypothesis. We measure both down- and upward deviations from SM !
 - χ^2 contribution calculated via inverse error function:
$$d\chi^2 = \text{Erf}^{-1}(1-CL_{2s}+B)$$

- Alternative treatment, followed here:

- χ^2 contribution is: $-2\ln Q$
- Lacks statistical information from experiments.
- No 2-sided interpretation
- ATLAS CL_S+B not public

- Note about combination of ATLAS and CMS $H \rightarrow WW$ results
 - Ignores correlations between x-section theory and luminosity uncertainties !
 - Tevatron/LHC combination procedure needed

